

```
(%i1) kill(all);
(%o0) done
```

1 Eq. (1)

1.1 with variable omega(u)

```
(%i1) depends([u,r],phi);
(%o1) [u(phi), r(phi)]
```

```
(%i2) E1: diff(u,phi,2)+u=omega(u)/(1+epsilon*cos(phi));
(%o2) 
$$\frac{d^2}{d\varphi^2} u + u = \frac{\omega(u)}{\epsilon \cos(\varphi) + 1}$$

```

```
(%i3) ode2(E1,u,phi);
(%o3) false
```

1.2 with constant omega_u

```
(%i4) E1: diff(u,phi,2)+u=omega_u/(1+epsilon*cos(phi));
(%o4) 
$$\frac{d^2}{d\varphi^2} u + u = \frac{\omega_u}{\epsilon \cos(\varphi) + 1}$$

```

```
(%i5) assume(epsilon^2-1<0);
(%o5) [ $\epsilon^2 < 1$ ]
```

```
(%i6) ode2(E1,u,phi);
(%o6) 
$$u = \left( \sqrt{1-\epsilon^2} \left( 2 \omega_u \sin(\varphi) \operatorname{atan}\left(\frac{\sin(\varphi)}{\cos(\varphi)+1}\right) + \omega_u \cos(\varphi) \log(\epsilon \cos(\varphi)+1) \right) - 2 \omega_u \sin(\varphi) \operatorname{atan}\left(\frac{\sqrt{1-\epsilon^2} \sin(\varphi)}{(\epsilon+1) \cos(\varphi)+\epsilon+1}\right) \right) / (\epsilon \sqrt{1-\epsilon^2}) + \%k1 \sin(\varphi) + \%k2 \cos(\varphi)$$

```

2 Eq. (2)

```
(%i7) E2: diff(u,phi,2)+u=1/alpha*(1+omega_u/u);
(%o7) 
$$\frac{d^2}{d\varphi^2} u + u = \frac{\frac{\omega_u}{u} + 1}{\alpha}$$

```

```
(%i8) ode2(E2,u,phi);
```

```
(%o8) [ - ∫  $\frac{1}{\sqrt{\frac{2 \omega_u \log(u) - \alpha u^2 + 2 u - 2 \%k1}{\alpha}}} du = \varphi + \%k2,$ 
```

```
∫  $\frac{1}{\sqrt{\frac{2 \omega_u \log(u) - \alpha u^2 + 2 u - 2 \%k1}{\alpha}}} du = \varphi + \%k2]$ 
```

□ **3 Eq. (5)**

```
(%i9) E5: diff(u,phi,2)+u=omega_u*(1-epsilon*cos(phi));
```

```
(%o9)  $\frac{d^2}{d\varphi^2} u + u = \omega_u (1 - \epsilon \cos(\varphi))$ 
```

```
(%i10) res: ode2(E5,u,phi);
```

```
(%o10)  $u = -\frac{\epsilon^2 \omega_u \varphi \sin(\varphi) + (\epsilon^2 + 1) \omega_u \cos(\varphi) - 2 \epsilon \omega_u}{2 \epsilon} + \%k1 \sin(\varphi) + \%k2 \cos(\varphi)$ 
```

```
(%i11) res1: expand(ev(res,[phi=%pi/2, %k1=0]));
```

```
(%o11)  $u = \omega_u - \frac{\pi \epsilon \omega_u}{4}$ 
```